

Excellent quality (typeset work): recommended!

able

$$X(z) = \frac{1}{1 - .5z^{-1}}, \quad |z| > .5$$

Problem 2

$$X(z) = \sum_{n=-\infty}^{\infty} a^{|n|}$$

$$X(z) = \sum_{n=-\infty}^{-1} (az)^{-n} +$$

$$X(z) = \sum_{n=0}^{\infty} (az)^n - 1 +$$

$$X(z) = \frac{1}{1 - az} - 1 +$$

$$X(z) = \frac{1 - a^2}{(1 - az)(1 - a/z)}$$

$$ROC : |a| < |z| < \infty$$

Good quality (handwritten work): Acceptable

$$Y_d(e^{j\Omega T}) ; |\Omega| < \pi/T$$

; otherwise

$$Y_d(e^{j\Omega T}) = T \times H_d(e^{j\Omega T}) \times \frac{1}{T} X_c(j\Omega)$$

$$= H_d(e^{j\Omega T}) X_c(j\Omega) ; |\Omega| < \pi/T$$

$$\frac{Y_d(e^{j\Omega T})}{X_c(j\Omega)} = H_d(e^{j\Omega T})$$

$$\frac{e^{j\Omega T/2} - e^{-j\Omega T/2}}{T}$$

$$\frac{j \sin(\Omega T/2)}{T} ; |\Omega| < \pi/T$$

$$\frac{\sin(\Omega T/2)}{T} ; |\Omega| < \pi/T$$

Poor quality (handwritten work): Unacceptable!

-- Use darker pencil and improve the scan image quality

causal LTI system with input $x[n]$ and output $y[n]$ described by $y[n] = 2y[n-1] + x[n]$. Find the impulse response of the system $h[n]$. Is the system stable?

$$y[n-1] + x[n]$$

Z transformation

$$z^{-1}Y(z) + X(z)$$

$$z^{-1}Y(z) = X(z)$$

$$2z^{-1}Y(z) = X(z)$$

$$\frac{Y(z)}{X(z)} = \frac{1}{1 - 2z^{-1}}$$

1/ z^{-1} - Z transformation

Not converted to black-and-white images, hard-to read handwriting (handwritten work): Unacceptable!

The given sequence is non-zero otherwise the sequence is,

$$x[n] = -\left(\frac{1}{2}\right)^n$$

To find the Z-transform, we

$$X(z) = \sum_{n=-\infty}^{\infty} x[n] z^{-n}$$

Since $x[n] = 0$ for $n > 0$, we
 $n = -\infty$ to -1

$$X(z) = \sum_{n=-\infty}^{-1} -\left(\frac{1}{2}\right)^n$$

We can change the index $k =$
Standard geometric series

$$k = -n \Rightarrow n = -k,$$